

MODEL QUESTION PAPER
MATHEMATICS

MAX: Score: 80
Time: 2 ½ hrs.

1. Consider the universal set $U = \{x : x \text{ is a natural no. } 1 \leq x \leq 10\}$

$A = \{x : x \text{ is an even natural no. } 1 \leq x \leq 10\}$

$B = \{x : x \text{ is a prime no, } 1 \leq x \leq 10\}$

i) Write A and B in roster form (1 + 1)

ii) $A \cup B$ ii) Verify $(A \cup B)' = A' \cap B'$ (1 + 2) (5)

2. A real valued function f is defined by $f(x) = \frac{3}{x-3}$

i) Find the domain of f

ii) Find the range of f

iii) Find $f(-4)$ (3)

3. Let $A = \{1,2,3\}$, $B = \{3,4\}$ and $C = \{4,5,6\}$ Find

i) $A \times (B \cap C)$ ii) $(A \times B) \cap (A \times C)$ 1 + 1 ½ + ½

iii) Verify that $A \times (B \cap C) = (A \times B) \cap (A \times C)$ (3)

4. i) Find the degree measure of $\frac{3\pi}{2}$

ii) Prove that $\frac{\sin 5x + \sin 3x}{\cos 5x + \cos 3x} = \tan 4x$

iii) Solve $2 \cos^2 x + 3 \sin x = 0$ 1 + 2 + 3 (6)

5. Consider the statement $P(n): 1 + 3 + 3^2 + \dots + 3^{n-1} = \frac{3^n - 1}{2}$

i) ~~P.T~~ $P(1)$ is true

ii) Using the Principle of Mathematics induction show that $P(n)$ is true for any natural no. n . 1 + 3 = 4

6. i) Convert the complex number $\frac{1+3i}{1-2i}$ in $a+ib$ form

ii) Convert the complex number $1 - i\sqrt{3}$ into Polar form 2 + 3 = 5

7. i) Solve $3(2-x) \geq 2(1-x)$

ii) Solve the following system of inequalities graphically

$$2x+y \geq 6$$

$$3x+4y \leq 12$$

$$x \geq 0, y \geq 0$$

2+

8. 1) A polygon has 44 diagonals. Find its number of sides

2) The letters of the word 'PARAMU' are permuted among themselves and arranged as if in a dictionary. Find the Rank of the word PARAMU

3) If ${}^n C_7 = {}^n C_5$ find the value of n

9. 1) Find the term independent of x in the expansion of

$$\left(\frac{3}{2}x^2 - \frac{1}{3x}\right)^6$$

2. Find the number of terms in the expansion of $(1-x)^{100}$

10. Consider the series $3.5 + 5.7 + 7.9 + \dots$

a) 1. Write the n^{th} term of the series

2. Find sum of first 'n' terms

b) Find the three consecutive terms in a G.P. whose sum is $39/10$ and product is 1

11. 1) Consider the straight line $3x + y - 8 = 0$ Reduce it to the normal form and find the values of 'P' and ω

2) Find the ratio in which the line $x+y=4$ divides the join of the points $(-1,1)$ and $(5,7)$

3) Find the co-ordinates of the dividing points

12. 1) Find the eccentricity, foci, directrix and length of Latus rectum of the hyperbola $36y^2 - 9x^2 = 144$

2) Find the equation of the parabola passing through $(2,5)$ and Symmetric along the x -axis

13. 1) Name the octant in which the point (1,2,3) lies 1

2) Find the ratio in which the line joining the points (-1,0,2) and (3, 4, -5) crosses the XY plane. 2

3) Show that the points (-2, 3,5), (1,2,3) and (7,0,-1) are collinear 1

14. 1) Evaluate $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - 1}{x}$ 2

2) Using first principles, find the derivative of $\tan x$ 2

3) Differentiate $\sin 2x$ with respect to x 2

15. 1) Consider the statement, "If 'x' is an even number Then 'x' is divisible by 4". Write its converse and Contrapositive 2

2) Prove by contradiction method that the statement "the sum of an irrational number and a rational number is irrational" is valid 2

16. Consider the following frequency distribution

Classes	30 – 40	40 – 50	50 – 60	60 – 70	70 – 80	80 – 90	90 - 100
Frequency	3	7	12	15	8	3	2

1) Find the mean

2) Find standard deviation

3) Find coefficient of variation (2+2+1 = 5)

17. If E and F are events such that $P(E) = \frac{1}{4}$, $P(F) = \frac{1}{2}$, $P(E \text{ and } F) = \frac{1}{8}$ Find

1) $P(E \text{ or } F)$

2) $P(\text{not } E \text{ and not } F)$ 2+2 = 4

Prepared by Ernakulam Cluster – Group 3.

SHABANA SHARAF	(07143)
MANJU M	(07006)
SHAJIRA A	(07032)
SONIA A.V	(07020)
BISINI K.A.	(07037)
SAHEERA I	(07071)
DEEPA.M	(07071)
MARGARET SALAY K.S	(07070)
SAUMYA CLEETUS	(07067)
ANTONY JOSEPH	(07004)
BIJU GEORGE	(07063)
NEELIMA AUGUSTINE	(07063)
VIJIMOLE VARGHESE	(07034)
SHAMEENA.S	(07034)